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W.M. Phillip Hudelson* (phil.hudelson@gmail.com), 411 Waupelani Drive, APT A-301,
State College, PA 16801. *Strong separations and Kolmogorov complexity.*

We prove using a forcing argument a new strong separation for partial randomness, which is equivalent to the following non-extraction result for Kolmogorov complexity: Let $f : \mathbb{N} \rightarrow [0, \infty)$ be a recursive and unbounded function such that $f(n+1) \leq f(n) + 1$ for all n and $\lim_{n \rightarrow \infty} (n - f(n)) = \infty$. Then there is an X such that $K(X \upharpoonright n) \geq f(n)$ for all n , but no Y recursive in X satisfies $K(Y \upharpoonright n) \geq f(n) + 2 \log_2(f(n)) + O(1)$ for all n . Here X and Y are infinite sequence of 0's and 1's, $X \upharpoonright n$ denotes the length n initial segment of X , and K denotes prefix-free complexity. This theorem generalizes the theorem of Miller (*Advances in Mathematics*, 226 (1): 373–384, 2011) that there exists a Turing degree of effective Hausdorff dimension $1/2$. (Received February 20, 2013)